## STA 141A: Homework 5

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The assignment must be done in an R Markdown or Quarto document. The assignment must be submitted by the due date above by uploading:

• a .pdf file in GRADESCOPE (if you can knit/compile your .rmd to a .html file only, please save the created .html file as a .pdf file (by opening the .html file -> print -> save to .pdf)).

Email submissions will not be accepted.

Each answer has to be based on R code that shows how the result was obtained. The code has to answer the question or solve the task. For example, if you are asked to find the largest entry of a vector, the code has to return the largest element of the vector. If the code just prints all values of the vector, and you determine the largest element by hand, this will not be accepted as an answer. No points will be given for answers that are not based on R. This homework already contains chunks for your solution (you can also create additional chunks for each solution if needed, but it must be clear to which tasks your chunks belong).

There are many possible ways to write R code that is needed to answer the questions or do the tasks, but for some of the questions or tasks you might have to use something that has not been discussed during the lectures or the discussion sessions. You will have to come up with a solution on your own. Try to understand what you need to do to complete the task or to answer the question, feel free to search the Internet for possible solutions, and discuss possible solutions with other students. It is perfectly fine to ask what kind of an approach or a function other students use. However, you are not allowed to share your code or your answers with other students. Everyone has to write the code, do the tasks and answer the questions on their own.

During the discussion sessions, you may be asked to present and share your solutions.

### 1. Logistic Regression with the titanic dataset

Use the following codes to download the titanic data, which provide information on the fate of passengers of Titanic.

```
install.packages("titanic") # run just once, then comment out
library(titanic) # run every time
```

(a) Fit a logistic regression model using the titanic\_train dataset, with Survived as the response variable. Use passenger class, sex, age, and fare as predictors. Which predictors are significant, with significance level  $\alpha = 0.05$ ?

### Your Solution (Code)

(b) Predict the survival status (binary) using the titanic\_test dataset. What portion of passengers are predicted to survive?

### Your Solution (Code)

#### 2. Logistic Regression by hand

We would like to individuals with a certain balance to the class "default" or to "no default" by using logistic regression. We calculated the estimates  $\hat{\beta}_0 = -10.4$  and  $\hat{\beta}_1 = 0.007$  for the true, but unknown parameters  $\beta_0$  and  $\beta_1$  in the logistic regression model, respectively. To which class would you assign individuals with balances X = \$1,000 and X = \$1,750, given that we conservatively assign individuals with balance X = x to the class "default" if  $P(X = x) \ge 0.2$ .

## 3. Odds by hand

ISLR2 Section 4.8 Exercise 9

# 4. Log odds by hand

ISLR2 Section 4.8 Exercise 12

### 5. Discriminant functions by hand

We would like to analyze the effect of the number of hours regularly working a day in front of a laptop (modeled by X) on concentration (modeled by Y). We distinguish between full concentration ability (class "1"), mild concentration difficulties (class "2") and severe concentration difficulties (class "3"). We have the following data:

$$(10, 2), (5, 2), (5, 3), (6, 1), (11, 2), (12, 3), (13, 2), (9, 2), (3, 1), (2, 1).$$

a. Calculate the discriminant functions for each of the three classes.

b. Explain to which class you would assign people who regularly work x = 4, x = 7, x = 14 hours per day in front of a laptop.